## Station 1: Proof Practice

Use the statements and reasons provided to complete the proof. Mark the diagram first!
Given: $\overline{W Y}$ is an altitude of $\triangle X Y Z$
$\overline{W Y}$ is an angle bisector $\triangle X Y Z$
Prove: $\angle X \cong \angle Z$


| Statements |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\overline{W Y} \cong \overline{W Y}$ | $\overline{W Y} \perp \overline{X Z}$ | $\angle Y W X \cong \angle Y W Z$ | $\overline{W Y}$ is an altitude of <br> $\Delta X Y Z$ | $\angle Y W X$ and $\angle Y W Z$ <br> are right angles |
| $\overline{W Y}$ is an angle <br> bisector $\Delta X Y Z$ | $\Delta X Y W \cong \Delta Z Y W$ | $\angle X \cong \angle Z$ | $\angle X Y W \cong \angle Z Y W$ |  |


| Reasons |  |  |  | CPCTC | Reflexive POC |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Given | $\begin{array}{c}\text { If two segments are perpendicular, } \\ \text { then they form right angles }\end{array}$ | $\begin{array}{c}\text { If two angles are right angles, then } \\ \text { they are congruent }\end{array}$ |  |  |  | \(\left.\begin{array}{c}If a segment is an angle bisector, <br>

then it divides an angle into 2 <br>
congruent angles\end{array}\right]\)

| Statements | Reasons |
| :--- | :--- |
| 1. | 1. |
| 2. | 2. |
| 3. | 3. |
| 4. | 4. |
| 5. | 5. |
| 6. | 6. |
| 7. | 7. |
| 8. | 8. |
| 9. | 9. |

Fill in the blanks to complete the proof. Mark the diagram first!
Given: $I$ is the midpoint of $\overline{E G}$ $\angle E \cong \angle G$

Prove: $\overline{E G}$ bisects $\overline{H F}$


| Statements | Reasons |
| :---: | :---: |
| 1. $I$ is the midpoint of $\overline{E G}$ | 1. |
| 2. | 2. If a point is a midpoint of a segment, then |
| 3. $\angle E \cong \angle G$ | 3. Given |
| 4. $\angle G I F$ and $\angle E I H$ are vertical angles | 4. |
| 5. | 5. If two angles are vertical angles, then |
| 6. $\Delta$ | 6. If corresponding $\qquad$ of two triangles are congruent, then the triangles are congruent |
| 7. $\overline{I H} \cong \overline{I F}$ | 7. |
| 8. $\overline{E G}$ bisects $\overline{H F}$ | 8. If a segment divides a segment into two congruent segments, then $\qquad$ |

## Station 2: Drawing Special Segments

1. Fill in the blanks to review how to draw each special segment.

- To draw a median of a triangle, you need to find the $\qquad$ of the opposite side. The median has endpoints at a $\qquad$ of the triangle and the midpoint of the opposite side.
- To draw an altitude, you need to find the $\qquad$ of the opposite side. Begin at the vertex of a triangle and use the $\qquad$ slope of the opposite side to draw the altitude.
- To draw a perpendicular bisector of a side of a triangle, you need to find the midpoint and the $\qquad$ of the side. Begin at the $\qquad$ and use the opposite $\qquad$ slope of the side to draw the perpendicular bisector.

2. The vertices of $\triangle P Q R$ are at $P(3,-1), Q(0,-2)$, and $R(-4,4)$. Graph $\triangle P Q R$ and label its vertices. Then draw median $\overline{P M}$. Label $M$.

3. The vertices of $\triangle P Q R$ are at $P(0,0), Q(2,6)$, and $R(5,5)$. Graph $\triangle P Q R$ and label its vertices. Then draw the perpendicular bisector of $\overline{P Q}$.

4. The vertices of $\triangle A B C$ are at $A(2,3), B(5,1)$, and $C(1,-3)$. Graph $\triangle A B C$ and label its vertices. Then draw altitude $\overline{A H}$. Label $H$.

5. The vertices of $\triangle S T U$ are at $S(-4,2), T(1-1)$, and $U(-4,-4)$. Graph $\triangle S T U$ and label its vertices. Then draw the altitude from $T$.


What is the length of the altitude from $T$ ?

1. Identify each special segment as a median, angle bisector, perpendicular bisector, or altitude.
a)

b)

c)

d)

2. $\overline{Y B}$ is an altitude of $\triangle X Y Z$ and $m \angle Y B Z=(7 x+27)^{\circ}$. Find the value of $x$.

3. $\overline{A M}$ is a median of $\triangle A B C$. Draw the median in the diagram. If $B M=10 x-8$ and $C M=3 x+34$, find the value of $x$ and $C B$.

$x=$ $\qquad$ $C B=$ $\qquad$
4. Given $\overline{P S}$ is a median. Find $m \angle P S R$.

$m \angle P S R=$ $\qquad$ Classify $\triangle P R S$ by angles and sides: $\qquad$
5. In a diagram shown, $\overline{U V}$ is a perpendicular bisector of $\triangle S V W$ and $\overline{W V}$ is an angle bisector of $\Delta S W T$. Mark the diagram with the given information and then solve for $x, y$, and $m \angle S W T$.
$m \angle S W T=$ $\qquad$


## Station 4: The Triangle Inequality Theorem

Is it possible to form a triangle with the given side lengths? If not, explain why not.

1. $2 f t, 3 f t, 4 f t$
2. $2 m, 12 m, 10 m$
3. $7.5 \mathrm{in}, 9 \mathrm{in}, 1$ in

Find the range for the measure of the third side of a triangle given the measures of two sides.
4. $5 f t, 9 f t$
5. 7 in, 14 in.

Find the range of possible measures of $x$ if each set of expressions represents measures of the sides of a triangle. 6. $(x+1)$ yds., 5 yds., 7 yds.
$7.12 \mathrm{ft}, 20 \mathrm{ft},(2 k+4) \mathrm{ft}$

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1. Find the indicated angle measures.
$m \angle 1=$ $\qquad$ $m \angle 2=$ $\qquad$ $m \angle 3=$ $\qquad$

2. Fill in the blank with sometimes, always, or never.
a. The acute angles of a right triangle are $\qquad$ supplementary.
b. The acute angles of a right triangle are $\qquad$ complementary.
c. There can $\qquad$ be two right angles in a triangle.
d. A right triangle is $\qquad$ an isosceles triangle.
3. Find $m \angle F$.

4. List the angles in order from smallest to largest.

5. List the sides in order from smallest to largest.

6. Find the value of $x$ and the following angle measures.
$x=$ $\qquad$
$m \angle A=$ $\qquad$ $m \angle B=$ $\qquad$

$$
m \angle A C B=
$$ exterior angle $=$ $\qquad$

Classify $\triangle A B C$ : $\qquad$


## Station 6: Isosceles and Equilateral Triangles

1. Find the indicated angle measures.
$m \angle C A D=$ $\qquad$ $m \angle A C D=$ $\qquad$
$m \angle A C B=$ $\qquad$ $m \angle A B C=$ $\qquad$
2. Find the value of $x$. Then classify the triangle by its sides and angles.


$$
x=
$$

$\qquad$
3. Find the value of $x$. Then classify the triangle by its sides and angles.


$$
x=\ldots \quad m \angle A=
$$

Classification: $\qquad$
4. $\triangle F G H$ is an equilateral triangle with $F G=(x+5)$ in., $G H=(3 x-9)$ in. and $F H=(2 x-2) i n$. Find the value of $x$ and $F G$. (Draw a diagram to help!)

$$
x=
$$

$\qquad$ $F G=$ $\qquad$
5. Find the values of $x$ and $y$ in the diagram shown.


